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1 Peers, Bullying and School Performance: Exploring the Role of 2 Friendships

3 Tatiane Almeida de Menezes¹, Rute Alves da Cunha², Tatiane Almeida de Menezes³
4 and Isabel Pessoa De Arruda Raposo⁴

5 ¹ Universidade Federal de Pernambuco

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7 **Abstract**

8 Evidence in studies from different fields point to the harmfulness of being bullied on indicators
9 of success in an individual's life. Aiming to measure and understand the impact of this
10 inherently social event, this paper investigates how the friendships of lower secondary
11 education students in the city of Recife influence their likelihood of being victims of such a
12 phenomenon and its effect on the academic performance of these students. The two-stage least
13 squares method is applied to an IV-SLX model, using indirect friendship ties as an
14 instrument, and significant results are found at 95

16

17 **Index terms**— bullying. peer effects. school performance. spatial econometrics. instrumental variable.

18 **1 Introduction**

19 Bullying is a phenomenon recognized worldwide for its perverse effects. It can be observed in different spheres
20 where there is social interaction, such as education and work environments. Specifically focused on the school
21 setting, there are evidences that quantify the magnitude of the negative repercussions of bullying on the academic
22 performance of students who are victims (KIBRIYA et al., 2015; OLIVEIRA et al., 2018), pointing out its
23 harmfulness.

24 Still in the context of the school environment, it is pertinent to highlight the role of friendships in the classroom.
25 A positive association was found between the grades of the group of friends to which a student belongs and the
26 grades of this individual (RAPOSO et al., 2019). This is an important indicator that suggests the potential of
27 friendship networks as a means to achieve academic success, under the proper stimuli.

28 This work proposes to contribute to the thesis that the school environment and peer effects are fundamentals
29 for their performance. Having friends or being part of a particular group can directly impact the chances of a
30 student being bullied or not. In this sense, we seek to measure the probability of being bullied based on the
31 context effects and peer effects. For instance, we are working with a unique dataset that comes from a survey
32 carried out in 2017 and 2018 by the Fundação Joaquim Nabuco -FUNDAJ, a research institute that integrates
33 the Brazilian Ministry of Education.

34 To deal with the reflexive problem (MANSKI, 1993) present in peer effect estimation we are applying a Spatial
35 Lag Model of X with Instrumental Variable (SLX-IV) and as instrument we are using the lagged classroom
36 friendships weight matrix (BRAMOULLÉ et al., 2009).

37 In addition to this Introduction, this article consists of five more parts. The first contextualizes the topics
38 of bullying and peer effects according to the scientific literature in the fields of Economics, Psychology and
39 Psychiatry. In the section tree we describe the dataset and the empirical strategy. In the fourth part, the results
40 are presented with a brief discussion about them. Finally, we present some conclusion.

41 2 II.

42 3 Theoretical Framework

43 Bullying is defined as a form of violence (verbal or physical) that happens in a repetitive and persistent way,
44 addressed against one or more colleagues, characterized by targeting the weakest in order to intimidate, humiliate
45 or mistreat those who are targets of these aggressions (BULLYING, 2020). Bullying not only occurs in different
46 ways, but can also have serious impacts on the physical integrity, psychological health and even academic
47 performance and professional future of its victims. Studies have searched to identify the relation and the
48 magnitude of the effect, between being bullied or performing bullying in the school environment and student
49 achievement. Kibriya et. al (2015), for example, find that being bullied weekly at school negatively influences
50 students' math scores. Ponzo (2013) establishes a binary variable that indicates whether the student has had
51 something stolen from him or herself or if he or she has been bullied or hurt by another student. The author
52 also finds a negative relation between exposure to bullying and academic performance; especially in the case of
53 those who have had something stolen from them and who, among these, have been pressured by classmates to do
54 something they did not want to do. Additionally, a result that is worth pointing out is the prevalence of bullying
55 in larger classes.

56 Impacts on psychic health were also investigated. Kumpulainen et al. (2001) found that most children actively
57 or passively involved in bullying had some psychiatric disorder, such as depression, anxiety, fears, attention deficit
58 disorder, and psychosomatic symptoms. It is worth noting that such disorders were more common among those
59 who practice bullying and those who, in addition to practicing, are also victims. In the long term, Klomek et al.
60 (2015) observed that victims are at high risk of developing psychological problems, and perpetrators tend to be
61 involved in crime, specifically violent crimes and illicit drug use.

62 Due to its viscerally social character, it is important to explore the way in which bullying travels social
63 interactions. Oliveira et. al (2018) highlight that social skills and emotional stability play an important role in
64 reducing the likelihood of a student being bullied. Fekkes et al. (2006) even recommend, in their study, that
65 children with anxiety, depression or some other factor that makes them susceptible to victimization by bullying,
66 such as having few friends, not being popular or being under assertive, should be referred to a psychology
67 professional to be educated in social skills as a means of preventing bullying. This recommendation is reinforced
68 by the study by Sharp (1996), which, in addition to this strategy, exposes the importance of involving colleagues
69 in combating and preventing bullying.

70 In addition to the perceptible relevance of direct social interactions, there is also the indirect factor of
71 responding to peer pressure. It is possible to imply, based on Bursztyn et al. (2015), that there is a need
72 to keep up appearances because of the expectation of classmates. Students with excellent academic performance
73 purposely lowered their performance when they were told that their peers would know their grades (BURSZTYN
74 ET AL., 2015). This may be linked to the apprehension of being bullied and being labeled a nerd. Woods et al.
75 (2004) explore bullying in two aspects: the relational, such as the exclusion an individual from the group, and
76 the direct characterized by aggressiveness and the practice of direct violence against the victim. They find that
77 students who experience relational bullying are nearly three times as likely to have lower-than-expected academic
78 results.

79 Studies in the area of social networks and peer effects have been carried out in the field of Education Economics.
80 Through different methods, research has often reached the same result: there is a positive impact of the academic
81 performance of colleagues on the performance of an individual who is part of the group ??CALVÃ?"-ARMENGOL
82 et al., 2009; HANUSHEK et al., 2003; RAPOSO et al., 2019). In addition, Sund (2009) points out that this effect
83 may not be linear for all types of students, since he finds that students with low academic performance benefit more
84 from living with colleagues whose performance is higher. Similarly, Vardardottir (2013) shows that, when students
85 are placed in classes with students who have higher average ability, this generates a positive and significant effect
86 on the grade of these students. When lowachieving students are found together, a negative effect is perceived
87 (LAVY; SILVA; WEINHARDT, 2012). From the perspective of the duration of friendship links, Patacchini et
88 al. (2017) show that connections lasting more than a year tend to positively influence an individual's academic
89 results in the long term.

90 Given all of the mentioned, then, it can be seen that the friendship networks are crucial information of an
91 individual's social skills and susceptibility being bullied or performing bullying. For this reason, such a topic
92 proves to be of great relevance to be studied.

93 4 III.

94 5 Model a) Data Set

95 Data for this study derive from a survey carried out in 2017 and 2018 by the Fundação Joaquim Nabuco -
96 FUNDAJ, a research institute that integrates the Brazilian Ministry of Education. The research involved 6 th
97 and 7 th graders in public schools of the city of Recife and consisted of a panel with students that were closely
98 monitored during the two years of this survey. Students, their guardians, teachers and school principals answered
99 a detailed questionnaire that resulted in a very complete set of information related to school and out-ofschool
100 aspects, which included information related to the practice and experience of bullying, as well as friendship

101 networks in the classroom. In 2017, of the 3,274 respondents who took both tests, 21.28% answered in the
102 affirmative to the direct question about having been bullied during the period in which the survey was carried
103 out. Of the 3,170 in 2018, 19.64% reported being bullied. In order to assess school achievement, students took
104 math and a Portuguese tests at the beginning and ate the end of the school year, for both years of the research,
105 totaling four tests for each subject.

106 An important characteristic of the 6 th grade of Primary and Lower secondary education is that this is the
107 students' first year in the so-called "Middle School" (BRASIL, 2018, p.27). In the city of Recife, particularly,
108 children are almost always relocated to new schools during the transition from 5 th to 6 th grade, as could be
109 verified in the research: 87.56% of students declared that they were newcomers in 2017. This fact should be
110 especially highlighted in this paper because it is probable that, this year, students will form new friendships and
111 build bonds with each other; as well as they may be more susceptible to being bullied by older students, for
112 example. In its turn, in the 7 th grade, with more time of coexistence, the friendship bonds tend to be firmer
113 and some social dynamics may be adjusted.

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116 In this article, only data collected in 2018 is being used due to a few reasons: it is the most complete sample in
117 terms of the fit between answers to socioeconomic questions and those about friendships; it captures a second
118 moment in the school life of the students who participated in both periods, and their bonds of friendship are
119 firmer. By eliminating missing and outlier information, a total of 2,809 observations remained, a reduction of
120 only 11.38% of the initial sample in 2018.

121 The control variables are described in table 1. The outcomes are Portuguese and mathematics scores (from
122 0 to 100) of the tests applied at the end of each year. The variable representing bullying victimization is a
123 dummy, where it equals 1 when the student reports being bullied and 0 in another case. In the survey data, the
124 connections between students is also carried out, where they could point up to 5 other students as their friends.
125 In this way, it is possible to link one student to another, see their characteristics and generate inferences about
126 behaviors, influences, etc. It is worth mentioning that, even if an individual points to another as a friend, it
127 should not necessarily be assumed that this relationship was reciprocally informed. Therefore, there is a vast
128 and complex range of identified relationships.

129 **8 b) Empirical Strategy**

130 This paper proposes to contribute to the theory that the school environment and the students' friendship network
131 are essential to their performance. Having friends or being part of a certain group can directly impact the chances
132 of a student being bullied or not. In this sense, we seek to identify the impact of bullying on students' grades
133 according to the general equation described below: $Y_{it} = \beta_0 + \beta_1 \text{Bullying}_{it} + \beta_2 \text{Control}_{it} + \epsilon_{it}$ (1)

134 where Y_{it} are the educational outcomes, here, the Portuguese and mathematics grades of the student i in
135 the class t ; Bullying is represents the probability that the student i in the class t being bullied based on the
136 vulnerability of their friends being bullied 1, the vector Control_{it} , skcomprises a set of sociodemographic
137 attributes of the student i , being $k=6$ is the number of control variables used, already described in the Data
138 section: male, color, age, studies, security, and disciplined. The use of Spatial Econometrics is necessary here
139 because, in order to measure peer effects, it is necessary to insert the characteristics of the student's friends into
140 the equation, capturing their influence on the variable of interest. Such characteristics are represented by the
141 element Control_{it} , which includes the same six attributes mentioned, but for the
142 student i and k friends. This is a model classified as Spatial Lag Model of X (SLX), where the regression coefficient linked
143 to the weight matrix presents the effects of contextual or exogenous interactions. In this work, however, there is a
144 difficulty regarding the endogeneity caused precisely by the nature of social interactions. The student chooses his
145 friends for reasons of affinity according to his own individual characteristics; therefore, it is expected that such
146 attributes affect both the grade and the probability of being bullied. And the presence of complete interaction
147 prevents the identification of the effects of group outcomes from the influence of the exogenous characteristics
148 of its members (GIBBONS et al., 2014). In other words, the problem of reflection (MANSKI, 1993) exposes a
149 reality of back-and-forth, where the individual

153 **9 E**

154 influences his peers, who in turn also influence, as a group, the individual.

155 Following Bramoullé et al. (2009) our identification strategy is based on an instrumental variable using the
156 lagged classroom friendships weight matrix as instrument. The lagged friendship matrix provides a structure of
157 intransitive connections that are crucial for the identification of the peer effect. The intuition of this one is as
158 follows: consider a simple network with three students A, B and C. For assumption A and B are friends with each

11 RESULTS

159 other, as are B and C. However, A and C are not friends. So the only way C could influence A's behavior would
160 be through B. C's characteristics are therefore good instruments for the effect of B's behavior on A because
161 they certainly influence B's behavior, but they cannot influence directly the behavior of A (PATACCHINI &
162 VENANZONI, 2014).

163 In the first stage, the estimated equation can be described as below:?????????????????? ??,?? = ?? + ???? ????
164 ,?? 2 ????????????????? ?? ,?? + ? ?? ?? ?? ??? ,?? ?? ?? ,?? ?? 6 ??=1 + ? ?? ?? ?? ??,?? ?? 6 ?? =1 + ??
165 ??,??(2)

166 where, ?? ????, ?? 2 denotes the indirect friendship ties, that is, the matrix of weights of zeros and ones ??
167 ????, ?? , which, multiplied by itself, generates the lagged matrix used in this study. Thus, the element ?? ????
168 ,?? 2 Bullyingj, translates to the fact that friends of friends of ??, who are friends of ??, are bullied or not. The
169 component ?? ????, ?? 2 Bullying ??, ?? of equation (2) is the instrument considered in this study for the effect
170 of bullying suffered by ??.

171 In the second stage, the impact of the probability of being bullied on the student's academic performance is
172 measured as described in the equation below:?????? ??,?? = ?? + ??????????????????? ??,?? ? + ? ?? ?? ??
173 ????, ?? ?? ?? ?? ,?? ?? 6 ?? =1 + ? ?? ?? ?? ??,?? ?? 6 ??=1 + ?? ??,??

174 In which the independent variable represents the investigated educational outcomes: the scores obtained in
175 the Portuguese and mathematics tests applied at the end of the year. The other control variables are the same
176 as mentioned above.

177 In practice, two-stage least squares regression is performed using the single ivreg2 command in the STATA
178 statistical software, with sample adequacy, with school-level weights, previously using the svyset command based
179 on the 2017 sample. As the sample was stratified at the school level, the cluster option was used in all models
180 presented in the next section, in order to control for heteroscedasticity and obtain robust estimates of the variances
181 across the 87 clusters of schools, although there is a loss of efficiency.

182 10 IV.

183 11 Results

184 Table 2 shows the correlation between the probability of a student being bullied (dbbullied) relative to the chances
185 of their indirect friends being exposed to bullying (G2bullied), using a linear regression in which, to each column,
186 a control variable is added referring to characteristics of the individual's direct friends. 2 For the variable in the
187 first row, the results show significant coefficients at 1%, varying little as new variables are added to the model. In
188 this way, it appears that G2bullied is a strong candidate for an instrument for estimated bullying to be applied in
189 the second stage of the methodology. For both stages, robustness tests were applied to the model and its results.
190 The first is the model under-identification test, where the rejection of the null hypothesis suggests that the model
191 equation is correctly identified. For the model proposed in this work, the null hypothesis was rejected in both
192 regressions against the dependent variables. There is also the weak identification test, where the null hypothesis
193 translates that the instrumental variables used to estimate the endogenous variable are not really adequate to
194 fulfill this role. Here, in none of the regressions of the IV-SLX model, the Cragg-Donald Wald F statistic was less
195 than the Stock-Yogo critical values. Therefore, the instrument G2dbbullied is a good predictor for the endogenous
196 variable Wdbbullied. Then there is the weak instrument robust inference test, which seeks to assess whether there
197 are regressors that are not endogenous and that there is orthogonality. For this test, the results do not reject the
198 5% significance level.

199 In addition, the Generalized Method of Moments in Two Steps was used, with the option gmm2 in the
200 estimation, in order to ensure more robust and efficient tests regarding heteroscedasticity and autocorrelation.
201 The results reinforce those of the tests mentioned above. And, in the second stage specifically, Hansen's J statistic
202 test is applied, in which the null hypothesis seeks to identify whether the controls and instruments are valid, that
203 is, not correlated with the error term; the result here being that the equation is exactly identified.

204 Tables 3 and 4 describe the impact of the bullying variable on grades in Portuguese and Mathematics,
205 respectively. In both tables, column (1) corresponds to the result of the regression by OLS, this estimator being
206 theoretically biased. In column (3), the characteristics of the friends are inserted into the model, making it an
207 SLX. In columns (2) and (4), the instrument for the probability of being bullied according to indirect friendships
208 is applied; differing from the model of column (4) by the integration between the instrumental variable and
209 contextual effects (IV-SLX), which is the model proposed in this work. In all models, the characteristics of the
210 individual enter as control variables. The results in column (4) of Table 3 indicate that having an incremental
211 increase of 10% in the probability of being bullied can reduce the student's Portuguese grade by 2.23%, as the
212 dbbullied variable can assume values between 0 and 1. This reflects the thesis that being bullied is linked not
213 only to the characteristics of the individual, but to his/her network of friends as a whole: having friends or being
214 part of the socially appreciated or disappreciated circle of friends influences the chances of becoming a victim of
215 bullying that , in turn, impacts academic performance.

216 In Table 4, which describes the impact of being bullied on the math grade, column (4) informs the coefficient
217 value for the complete model, where increasing the chances of being bullied by 10% reduces the student's math
218 grade by 2.75%. Such evidence reinforces that there is a very strong social factor on the probability of becoming
219 a victim of bullying, and that it goes beyond the exogenous characteristics of the individual himself The results

220 measured here are in the same direction as the evidence found in the literature: Oliveira et. al (2018) also find a
221 negative impact of being bullied on the math grade of students in the same age group as the one considered here;
222 as well as Kibriya et. al (2015), but taking into account students of an older age group. From the perspective
223 of performance in linguistic knowledge, Ponzo (2013) identifies a negative relationship between the ability to
224 interpret texts and being a victim of bullying.

225 It is noted that in both results, the OLS model has a significant positive bias on the Portuguese score compared
226 to the other specifications; however, this does not make use of the instrumented variable, but of the data informed
227 by the individual about being bullied or not. Such a bias may suggest a few things: there is an omitted variable,
228 such as some physical characteristic not taken into account in this case, as well as being bullied as an individual
229 may be less harmful than having friends who are also victims.

230 In addition, we see a more intense perverse effect on the math grade than on the Portuguese grade. In the
231 survey, Portuguese is one of the subjects that students say they like more than they don't, unlike mathematics.
232 It is possible to speculate that being a good student in Portuguese may be more socially acceptable than in
233 Mathematics, since this subject is closely associated with being a nerd, a characteristic commonly linked to
234 victims of bullying.

235 V.

236 **12 Conclusion**

237 Given the evidence in the literature about the negative impact of the consequences of being bullied, both in the
238 short term and throughout an individual's life, we emphasized the need to investigate not only the magnitude
239 of this on the outcomes of success, but also through which paths it permeates. As it is an essentially social
240 phenomenon, it makes sense to observe its effects through networks of relationships.

241 In this study, we sought to measure, via a two stages least squares IV-SLX model, the effect of the probability
242 of being bullied based on the characteristics of the friendship networks of lower secondary education students in
243 the city of Recife, on two outcomes: Portuguese and Mathematics grades. The spatial lagged friendship matrix
244 was used as an instrument to deal with endogeneity that come from reflexive problem (MANSKI, 1993).

245 Significant and robust results were found in several tests that indicate a negative impact of bullying on the
246 student's school performance: by increasing the probability of being bullied by 10%, it decreases the Portuguese
247 and Math grades by 2.33% and 2.75%, respectively. Such indicators reinforce the argument of the degree of
248 importance given to relationship networks, and not just the characteristics of the individual, on the probability
249 of being a victim of bullying and suffering from the impact of its consequences in other areas of life.

250 Finally, this research tested the spatial lagged friendship matrix as an instrumental variable to identify the
251 impact of peer effects on the student's probability of being bullied and its effect on Portuguese and Math scores.
252 Indeed, this paper reinforces the necessity for a joint effort from areas such as Economics and Psychology, to
253 investigate and trace in detail the mechanisms that justify the results obtained here. ^{1 2 3}

¹In the survey of the network of friends in the classroom, the Fundaj Survey (2018) asked each student interviewed to list up to five best friends, who could or could not be in their class.

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³Variables starting with "G" are the control variables, specified in the Data section, spatially lagged.

12 CONCLUSION

1

Variable	Meaning	Average	Standard Devia- tion
N2_Portuguese	Student's Portuguese grade	37.28	18.71
N2_Mathematics	Student's Mathematics grade	36.71	20.14
dbbullied	Dummy if the student claimed to be bullied	0.16	0.37
age	Student Age	12.42	0.74
male	Dummy if the student is male	0.51	0.50
race	Dummy if the student is deemed to be white	0.20	0.40
studies	Frequency of student study	3.23	1.35
security	Dummy if the student feels safe in the neighborhood of residence	0.70	0.46
tdisciplined	Intensity of the teacher's perception of how disciplined the class is	2.17	0.66
Number of Observations	2869		

Figure 1: Table 1 :

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	(1)	G2dbbullied	0.249**	0.273**	(2)	Dependent Variable: dbbullied	(3)	(4)	(5)	0.305**	0.30
	(0.027)		(0.026)		(0.024)		(0.023)	(0.023)			
Gmale		-		-0.022		-	-	-	-		
			0.061**				0.023	0.023			
			(0.012)		(0.017)		(0.017)	(0.017)			
Gage				-0.004**	-0.005**	-0.006**	-0.007**				
				(0.001)			(0.001)	(0.002)			
Grace							0.024	0.024			

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[Note: * $p < 5\%$, ** $p < 1\%$.]

Figure 2: Table 2 :

3

	OLS	Dependent Variable: ln N2_Portugues	(2)	(3)	IV SLX
dbbullied	(1)				-0.286 *
male	-0.169	**			-0.168 **
	(0.051)				(0.113)
	-0.068 *				(0.055)
	(0.033)		(0.033)		(0.038)
race	-0.011		-0.018		-0.009
	(0.036)		(0.037)		(0.037)
age	-0.066 **		-0.066 **		-0.066
	(0.022)		(0.021)		**
studies	0.034 *		0.035 **		(0.021)
				0.033 *	

Figure 3: Table 3 :

3

Dependent Variable: ln N2_Portugues				
	(1)	(2)	(3)	(4)
OLS	IV	SLX		IV-SLX
	(0.013)	(0.013)	(0.013)	(0.014)
security	-0.003	-0.014	-0.000	-0.006
	(0.034)	(0.035)	(0.033)	(0.034)
tdisciplined	-0.067 *	-0.067 *	-0.049	-0.049
	(0.031)	(0.030)	(0.039)	(0.040)
Gdbullied			-0.087	
			(0.062)	
Gmale			-0.028	-0.028
			(0.025)	(0.026)
Gage			-0.001	-0.002
			(0.005)	(0.005)
Gstudies			0.010	0.010
			(0.014)	(0.014)
Gsecurity			0.064	0.073
			(0.057)	(0.053)
Grace			-0.028	-0.022
			(0.048)	(0.048)
Gdiscip			-0.022	-0.024
			(0.024)	(0.024)
_cons	4.405 **	4.424 **	4.370 **	4.368 **
	(0.318)	(0.310)	(0.329)	(0.324)
N	2803	2803	2803	2803
R 2	0.039	0.033	0.047	0.043
Statistics-F	10.72	8.12	10.96	6.49

Figure 4: Table 3 :

Dependent Variable: ln N2_Mathematics				
	(1)	(2)	(3)	(4)
	OLS	IV	SLX	IV-SLX
dbbullied	-0.036 (0.050)	-0.247 * (0.108)	-0.037 (0.051)	-0.275 * (0.113)
male	-0.019 (0.046)	-0.021 (0.044)	-0.008 (0.051)	-0.006 (0.049)
race	-0.004 (0.050)	-0.016 (0.052)	-0.002 (0.051)	-0.017 (0.053)
age	-0.028 (0.020)	-0.026 (0.022)	-0.025 (0.021)	-0.022 (0.024)
studies	0.011 (0.013)	0.013 (0.012)	0.009 (0.013)	0.012 (0.012)
safety	0.095 * (0.045)	0.076 (0.043)	0.096 * (0.044)	0.074 (0.042)
tdisciplined	-0.085 * (0.037)	-0.084 * (0.038)	-0.083 (0.046)	-0.086 (0.048)
Gdbbullied			-0.041 (0.062)	
Gmale			-0.023 (0.027)	-0.031 (0.026)
Gage			-0.005 (0.006)	-0.006 (0.006)
Gstudies			0.008 (0.011)	0.009 (0.011)
Gsecurity			0.088 * (0.040)	0.092 * (0.043)
Grace			-0.024 (0.050)	-0.018 (0.047)
Gdiscip			-0.000 (0.028)	0.003 (0.030)
_cons	3.890 ** (0.260)	3.917 ** (0.271)	3.844 ** (0.285)	3.869 ** (0.303)
N	2809	2809	2809	2809
R 2	0.013	-0.002	0.017	-0.002
Statistics-F	3.10	4.49	5.04	4.75

Standard error in parentheses. Statistics-F refers to the global model. Regression corrected for school-level effects.

[Note: * $p < 5\%$, ** $p < 1\%$.]

Figure 5: Table 4 :

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